Midterm Exam

(October 16th @ 5:30 pm)

Implement SAXPY (Single-Precision A.X Plus Y), also called Scaled Vector Addition with both pthreads and TBB.

$$\vec{v} \leftarrow a\vec{x} + \vec{v}$$

✓ SAXPY is a combination of scalar multiplication and vector addition. It takes as input two n-element input vectors \vec{x} and \vec{y} (whose elements are 32-bit floating point numbers), and a scalar value a. A simple C implementation looks like this:

```
void saxpy(int n, float a, float *x, float *y) {
  for (int i = 0; i < n; i++)
     y[i] = a*x[i] + y[i];
}</pre>
```

PROBLEM 1 (60 PTS)

- Implement SAXPY using pthreads in C (30 pts)
 - ✓ Your code should read the parameter *nthreads* (number of threads) and the length of the vectors (n).
 - Note that $nthreads \in [1, n]$.
 - ✓ Parallelization: each thread i ($i \in [1, n]$) computes a slice of the output vector \vec{y} with the following indices:
 - From $\left\lfloor \frac{i \times n}{nthreads} \right\rfloor$ to $\left\lfloor \frac{(i+1) \times n}{nthreads} \right\rfloor$.
 - \checkmark **Input data**: Given the length n_i , your code should initialize the vectors \vec{x} and \vec{y} as per the following pseudo-code:

```
a = 1.618
for i = 0:n-1
x[i] = \sinh(i*3.416/n); y[i] = \cosh(i*3.416/n);
```

✓ Verification: To be fully sure that your results are correct, you need to create a sequential implementation and then compare the results with those of your multi-threaded implementation. This can be achieved by computing the sum of absolute differences (SAD), which should be 0.0:

$$diff = \sum_{i=0}^{n-1} |y_p(i) - y_s(i)|$$

where \vec{y}_p and \vec{y}_s are the output vectors of the multi-threaded and sequential implementations respectively.

- Compile the code and execute the application on the DE2i-150 Board (or on a Linux laptop). Complete Table I (take an average of ~10 executions in order to get the computation time for each case). (20 pts).
 - ✓ Example: ./mysaxpy 1000 10
 - ^a It will compute SAXPY on 1000-element vectors \vec{x} and \vec{y} using 10 threads.

TABLE I. COMPUTATION TIME (US) VS. NUMBER OF THREADS AND VECTORS LENGTH

	nthreads									
n	1	2	3	4	5	6	7	8	9	10
1,000										
10,000										
100,000										
1,000,000										
2,000,000										

✓	Comment on your results in Table I. Is there an optimal number of threads? At what point increasing the number of
	threads causes an increase in processing time?

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Instructor: Daniel Llamocca

■ Take (and embed the image in your Midterm document) a screenshot of the software running in the terminal for nthreads=5, n=20. It should show the computation times (for both the sequential and the pthreads implementations), the input vectors \vec{x} and \vec{y} , the output vector \vec{y} , and the sum of absolute differences (SAD). Fig. 1 shows an execution example. (10 pts)

```
adaniel@daniel-Inspiron-1545: ~/Dropbox/mystuff/work_ubuntu/labs/midterm/saxpy_pthreads
x(input)
                v(input)
                                         y(output)
x[0]=0.0000
                y[0]=1.0000
                                         y[0]=1.0000
x[1]=0.1716
                                         y[1]=1.2923
                y[1]=1.0146
                y[2]=1.0589
                                         y[2]=1.6224
x[2]=0.3483
                y[3]=1.1342
                                         y[3]=2.0000
x[3]=0.5351
x[4]=0.7376
                y[4]=1.2426
                                         v[4]=2.4360
x[5]=0.9617
                y[5]=1.3874
                                         y[5]=2.9433
                y[6]=1.5727
x[6]=1.2138
                                         y[6]=3.5367
x[7]=1.5015
                y[7]=1.8040
                                         y[7]=4.2335
                y[8]=2.0881
                                         y[8]=5.0541
x[8]=1.8331
x[9]=2.2183
                y[9]=2.4333
                                         y[9]=6.0224
x[10]=2.6683
                y[10]=2.8496
                                         y[10]=7.1670
                y[11]=3.3492
                                         y[11]=8.5210
x[11]=3.1964
x[12]=3.8180
                y[12]=3.9468
                                         y[12]=10.1243
x[13]=4.5512
                v[13]=4.6598
                                         v[13]=12.0237
x[14]=5.4175
                y[14]=5.5091
                                         y[14]=14.2746
                y[15]=6.5194
x[15]=6.4423
                                         y[15]=16.9430
x[16]=7.6554
                y[16]=7.7205
                                         y[16]=20.1069
x[17]=9.0924
                y[17]=9.1473
                                         y[17]=23.8588
x[18]=10.7953
                y[18]=10.8416
                                         y[18]=28.3084
x[19]=12.8139
                y[19]=12.8529
                                         y[19]=33.5859
Sum of absolute differences: 0.0000
Time measurements
******
pthreads implementation - nthreads = 10
start: 555010 us
                        end: 555766 us
Elapsed time: 756 us
Sequential implementation
                        end: 556038 us
start: 556037 us
Elapsed time: 1 us
daniel@daniel-Inspiron-1545:~/Dropbox/mystuff/work_ubuntu/labs/midterm/saxpy_pthreads$
```

Figure 1. SAXPY execution showing three 20-element sets of values. Computation times obtained from execution on a Dell Inspiron laptop.

PROBLEM 2 (40 PTS)

- Implement SAXPY using TBB parallel for in C++ (15 pts)
 - ✓ Follow the same procedure as in Problem 1, but instead of using *pthreads* to implement slices of the output vector, use *parallel_for* to fully parallelize the sequential SAXPY. Make sure to include a sequential implementation in C++.
 - \checkmark Your code should read the parameter input data set size (n).
- Compile the code and execute the application on the DE2i-150 Board (or on a Linux laptop). Complete Table II (take an average of ~10 executions for each case). (15 pts)
 - ✓ Example: ./mysaxpy_tbb 1000
 - It will compute SAXPY on 1000-element vectors \vec{x} and \vec{y} .

TABLE II. COMPUTATION TIME (US) VS. VECTORS LENGTH

	n				
Implementation	10,000	100,000	1,000,000	2,000,000	5,000,000
Sequential					
TBB					

✓	Comment on your Table II results. Is there any point at which the TBB implementation is faster than the sequential one					
	Yes or No? If No, can you venture a guess as to why this is happening?					

■ Take (and embed the image in your Midterm document) a screenshot of the software running in the terminal for n=20. It should show the computation times (both sequential and the TBB implementations), the input vectors \vec{x} and \vec{y} , the output vector \vec{y} and the SAD (as in Fig. 1). (10 pts)

SUBMISSION

- Demonstration: In this Midterm, the requested screenshots of the software routines running in the Terminal suffices. You should embed the images in your Midterm document.
- Submit to Moodle (an assignment will be created):
 - ✓ Two <u>.zip</u> files (one for Problem 1 and one for Problem 2).
 - Problem 1: The .zip file must contain the source files (.c, .h, Makefile).
 - Problem 2: The .zip file must contain the source files (.cpp, .h, Makefile).
 - ✓ Your Midterm work (a PDF file): This must include the completed Tables I and II, your comments, as well as the requested screenshots (2).

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